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Unobserved heterogeneous effects in the cost efficiency analysis of electricity distribution systems*

Per J. Agrell², Mehdi Farsi³, Massimo Filippini⁴ and Martin Koller⁵

Abstract

The purpose of this study is to analyze the cost efficiency of electricity distribution systems in order to enable regulatory authorities to establish price- or revenue cap regulation regimes. The increasing use of efficiency analysis in the last decades has raised serious concerns among regulators and companies regarding the reliability of efficiency estimates. One important dimension affecting the reliability is the presence of unobserved factors. Since these factors are treated differently in various models, the resulting estimates can vary across methods. Therefore, we decompose the benchmarking process into two steps. In the first step, we identify classes of similar companies with comparable network and structural characteristics using a latent class cost model. We obtain cost best practice within each class in the second step, based on deterministic and stochastic cost frontier models. The results of this analysis show that the decomposition of the benchmarking process into two steps has reduced unobserved heterogeneity within classes and, hence, reduced the unexplained variance previously claimed as inefficiency.

Keywords: Efficiency analysis; cost function; electricity sector; incentive regulation

JEL classification: L92, L50, L25

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1 INTRODUCTION

In the last two decades the electricity distribution sector in Europe has witnessed a wave of regulatory reforms aimed mainly at improving the economic efficiency. Thereby, information on several efficiency concepts in production theory, including scale and scope efficiency as well as cost efficiency has become very important. The concept of cost efficiency is a measure of the regulated electricity distribution company's ability to minimize costs, given specific demand and market conditions. Cost inefficiency, also called 'X-inefficiency', occurs when the company fails to produce with full efficiency at the cost frontier, defined by best-practice companies.

Regulatory authorities increasingly use empirical cost norms, such as parametric or non-parametric benchmarking methods, in various incentive regulation schemes (Haney and Pollitt (2009)). One of the most widely used regulatory regimes in electricity networks is price- or revenue-cap regulation (often denoted CPI-X regulation, cf. Littlechild (1983)). This method determines a maximum price or revenue index in real terms, less a productivity improvement parameter, referred to as the 'X-factors'.⁶ The X-factors include a general productivity improvement requirement (usually called the 'general X-factor') and potentially an individual efficiency improvement parameter (frequently denoted the 'Xi-factor' or the individual X-factor). Whereas the purpose of the general X-factor is to share the productivity gains in the sector between the consumers and the companies, the individual factor is intended to remove incumbent efficiency differences between companies. The exact translation of an estimated static cost inefficiency to an annual real productivity target (X_i) depends on the allowed period to catch up inefficiency, the type of inefficiency detected (capital and/or operating costs) and the type of by-pass mechanism (Z) used for certain costs that may be proportional to the inefficiency (e.g. network losses). Notwithstanding, the mechanism allows the regulator to set differentiated price or revenue caps based on the individual company's empirically estimated productive efficiency performance.⁷ An alternative to the CPI-X regulation, addressing the arbitrariness of the adjustment parameters and the risk induced by the lag, is the yardstick regulation paradigm (cf. Shleifer (1985)). In this model, the reimbursement of the regulated firm is linked to a dynamic norm, excluding the cost report of the specific company in its calculation. Although Shleifer presented the model for a stylized cost function, the use of frontier analysis tools enables the application of yardstick methods also to multi-output production and service provision. Several regulators in Europe, thereof Germany and Norway, use DEA for dynamic yardstick regimes in electricity distribution regulation.⁸

⁶ In addition to inflation, the changes beyond companies' control may include changes in input factor prices and exogenous changes in demand and network characteristics, generally referred to as 'Z-factors'.

⁷ The level of productive efficiency or cost efficiency of a firm is composed by the levels of technical and allocative efficiency. For a discussion of these concepts see Kumbhakar and Lovell (2003).

⁸ The theory for dynamic applications of DEA in yardstick and a comparison with a conventional CPI-X approach are found in Agrell et al. (2005a).

However, the increasing use of efficiency analysis has raised serious concerns among regulators and companies regarding the reliability of efficiency estimates.⁹ In fact, empirical evidence suggests that the estimates are sensitive to the adopted efficiency measurement approach.¹⁰ This implies that the choice of the approach may have important effects on the financial situation of the companies as well as on the industrial structure of the regulated sector.

One important dimension affecting the reliability of efficiency estimates is the presence of *unobserved factors*. The regulated companies operate in different regions with various environmental and network characteristics that are only partially observed. This heterogeneity in the service area is an important factor to consider in a benchmarking analysis. Recall that the purpose of the benchmarking method is to create a cost norm for efficient, structurally comparable companies under similar operating conditions. Some methods of estimating efficiency take account for such unobserved factors, but in different ways. Generally, in deterministic models such as the non-parametric linear programming approach, the unobserved factors that influence the level of production costs are not considered in the analysis. The explicit assumption in these approaches is that all relevant cost differences are captured by observed variables. The few efficiency analysis models accounting for part of the unobserved heterogeneity factors are parametric and based on panel data. The seminal paper for the development of models for unobserved heterogeneous factors is Greene (2005). The main idea is to introduce an individual effect in an econometric model capturing the unobserved heterogeneous factors that remain constant over time. The main problem hereby is that the individual effects can capture also part of the inefficiency that remains constant over time. In addition, the complexity of the models developed by Greene (2005) and the entailed assumptions remain important obstacles in applying panel data models in regulatory practice. Given that the unobserved factors are considered differently in various models, the resulting estimates can vary across methods. The magnitude of variation depends on the importance of the unobserved factors, which might change from one case to another.

To address this problem, we propose an alternative strategy for improve efficiency measurement methodology in the presence of unobserved heterogeneity. In our strategy, we decompose the benchmarking process into two steps: In the first step, we attempt to identify classes of companies that operate in similar environments and with comparable network and structural characteristics. For this purpose, we apply a latent class model. In the second step, the best practice is obtained within each class, based on deterministic and stochastic frontier models. Provided that the identified classes contain reasonably comparable cases and assuming a reasonable explanatory power

⁹ Shuttleworth (2005) provides a critical overview of the problems coming along with the use of benchmarking in the regulation of electricity networks.

¹⁰ See e.g. Jamasb and Pollitt (2003), Estache et al. (2004), Farsi and Filippini (2004) or Farsi et al. (2006).

for the variables included in the model specification, any deterministic or stochastic approach can be used to estimate efficiency.

The outline of this Chapter is as follows: Section 2 reviews some of the most commonly used approaches to efficiency measurement. Section 3 addresses the cost model specifications and estimation methods. Section 4 introduces the data and Section 5 provides the estimation results for both steps and measures of cost efficiency for different frontier models in the second step. We draw our conclusions in Section 6.

2 REVIEW ON APPROACHES TO EFFICIENCY MEASUREMENT

This section briefly reviews some of the most commonly used frontier approaches to cost efficiency measurement, based on more extensive reviews in Kumbhakar and Lovell (2003), Murillo-Zamorano (2004), Coelli et al. (2005), Cornwell and Smith (2008), Greene (2008; Kumbhakar and Lovell (2003), and Farsi and Filippini (2009)).¹¹ The focus here is mainly on cost efficiency and on cost functions, the argumentation is analogously valid for production functions and productive efficiency (under a set of regularity conditions, cf. Shepard (1953) and Nerlove (1963)). The frontier approach assumes that full cost efficiency is defined by those companies that are identified as the best-practice peers. All other companies are assumed to operate above the cost frontier, hence to have non-zero inefficiency.

Economic literature has developed two different frontier paradigms to empirically measure cost efficiency.¹² The first is based on a non-parametric deterministic and the second on an econometric approach, sometimes also referred to the parametric approach.

Non-parametric approaches, such as the Data Envelopment Analysis (DEA), proposed by Farrell (1957) and Charnes et al. (1978)), use linear programming to construct a company's efficiency frontier, which is considered as a deterministic function of the observed variables. These methods are non-parametric in the sense that they do not impose any specific functional form or distribution assumption, i.e. it is assumed that the data are free of noise. Thanks to their relative simplicity and availability, such methods, in particular DEA, are quite popular among both researchers and regulators in energy distribution networks. The DEA models can be input- or output-oriented and one of the a priori assumptions concerns the returns to scale. The models can be specified as constant returns to scale (CRS), variable returns to scale (VRS), non-increasing returns to scale (NIRS), non-decreasing returns to scale (NDRS), free disposal hull (FDH) and free replicability hull (FRH), where the latter

¹¹ The latter review includes also sections on the traditional production theory and on scale and scope economies.

¹² A third paradigm, the Bayesian approach is only little-known in applied science. Readers interested in Bayesian stochastic frontier models (sometimes also assigned to non-parametric models) are referred to van den Broeck et al. (1994).

two merely imposes disposability and additivity, but not convexity of the production space. A basic DEA formulation calculating the minimal cost under VRS for company i in a sample of N companies with k inputs and m outputs would be

$$\begin{aligned} & \min_{\lambda, x_i} w_i' x_i \\ \text{s. t. : } & -y_i + Y\lambda \geq 0; \quad x_i - X\lambda \geq 0; \quad N'\lambda = 1; \quad \lambda \geq 0 \end{aligned} \quad (1),$$

where w_i and x_i are $k \times 1$ vectors representing input prices and quantities for company i ; y_i is an $m \times 1$ vector representing the given output bundle; X and Y are input and output matrices namely, a $k \times N$ and an $m \times N$ matrix consisting of the input and output bundles for all companies in the sample; N is an $N \times 1$ vector of ones; and λ is an $N \times 1$ vector of non-negative constants to be estimated. The VRS property is satisfied through the convexity constraint ($N\lambda=1$) that ensures that only similar-sized companies are benchmarked against each other. The linear programming algorithm finds a piecewise linear isoquant in the input-space, which corresponds to the minimum costs of producing the given output at any given point. Cost efficiency (CE) finally is measured by the minimum feasible input bundle for each company relative to its actual input bundle, i.e. $CE_i = w_i' x_i^* / w_i' x_i^0$.

In contrast to non-parametric methods, most of the econometric approaches include estimating an empirical cost function, where the observed variables should include a vector of outputs (\mathbf{q}) and a vector of input prices (\mathbf{p}). The remaining unobserved part, the residual, is completely (in deterministic models) or partially (in stochastic models) assigned to inefficiency.

The first econometric frontier models that appeared in the literature were deterministic and estimated by OLS. Usually, their cost function is expressed in logarithms as

$$\ln C_{it} = f(\mathbf{q}_{it}, \mathbf{p}_{it}; \boldsymbol{\beta}) + \alpha + \varepsilon_{it} \quad (2),$$

where C_{it} is total cost incurred by the unit i at time t , $f(\cdot)$ is a parametric cost function, \mathbf{q}_{it} and \mathbf{p}_{it} are vectors of outputs and input prices, respectively, $\boldsymbol{\beta}$ is the vector of parameters and α the intercept to estimate, and ε_{it} is the residual. As the error term in deterministic models only reflects the inefficiency, it is assumed to be non-negative. Therefore, Winsten (1957) suggested shifting the estimated intercept down by the minimal residual value. This model is called Corrected OLS (COLS). The cost efficiency of unit i in the COLS model is thus given by $\exp(-u_{it})$ with $u_{it} = \varepsilon_{it} - \min(\varepsilon_{it}) \geq 0$. Afriat (1972) proposed a slightly different model, usually referred to as Modified OLS (MOLS), where the OLS intercept is shifted by the expected value of the inefficiency term that is, $E(u_{it})$. The cost efficiency of unit i at time t in the MOLS model is thus given by $\exp(-u_{it})$ with $u_{it} = \varepsilon_{it} + E(u_{it})$. The efficiency term u_{it} is not necessarily positive (some units are below the cost frontier). Truncation at zero assigns the respective units with full efficiency.

Deterministic models are similar to DEA and other linear programming models in that the best practice (the cost frontier) is a fixed function that does not vary across observations or units. As main drawback, these models attribute the residual to inefficiency, i.e. they do not account for other sources of stochastic variation such as measurement errors.¹³ Nevertheless, deterministic models are still widely used in applied economic literature and in regulation (see e.g. Haney and Pollitt (2009)).

To overcome the drawbacks of deterministic models, Aigner et al. (1977) and Meeusen and van den Broeck (1977) proposed a stochastic frontier model (SFA), which divides the residual ε_{it} into two parts: u_{it} is reflecting inefficiency, and v_{it} is capturing the random noise. The basic cost function of the stochastic frontier model can be written as

$$\ln C_{it} = f(\mathbf{q}_{it}, \mathbf{p}_{it}; \boldsymbol{\beta}) + \alpha + u_{it} + v_{it} \quad (3).$$

With certain distribution assumptions on u_{it} and v_{it} , this model can be estimated using the Maximum Likelihood (ML) estimation method. Typically, it is assumed that the inefficiency term u_{it} has a one-sided non-negative distribution that is, a normal distribution truncated at zero: $u_{it} \sim |N(0, \sigma_u^2)|^{14}$, and the random noise term v_{it} is normally distributed: $v_{it} \sim N(0, \sigma_v^2)$. Additionally, u_{it} and v_{it} are considered as being independently distributed from each other. As in the models above, one would expect the most efficient unit to take $u_{it} = 0$, and the efficiency value to be calculated as $\exp(-u_{it})$. Unfortunately, $E(u_{it})$ cannot be calculated for an individual unit. Jondrow et al. (1982) proposed therefore a different estimator to measure efficiency. This estimator is based on the conditional expectation function of the residual, $(E[u_{it}|\varepsilon_{it}])$, and is known as the JLMS estimator referring to the authors.¹⁵ This is a highly non-linear function that only slightly increases the inefficiency for units close to the frontier leaving no unit with full efficiency. The other estimator proposed by these authors is based on the conditional mode $(M[u_{it}|\varepsilon_{it}])$ that normally assigns full efficiency to several units. It has been used much less in the empirical literature than the JLMS estimator.

The models described so far can be applied either to cross-sectional or panel data. However, the panel structure in the data is ignored, as these models require pooling all observations and treating them as being independent from each other. Temporal variations can be captured using time trends or time-interactions. Moreover, these models are not suited to account for unmeasured, i.e. unobserved heterogeneity. This is due to the fact that with pooled data, each observation is considered

¹³ Semi-parametric frontier models such as quantile regression (Koenker and Bassett (1978)) sometimes count as deterministic models. Unlike least squares methods, quantile regression techniques do not approximate the conditional mean of the response variable, but either its median or quantiles and offer therefore a systematic strategy for examining the entire distribution of the population. Readers interested in applied quantile regression models for efficiency measurement are referred to Behr (2010) and to Knox et al. (2007).

¹⁴ Other extensions of the SFA model have considered exponential, gamma, or truncated normal distributions for the inefficiency term.

¹⁵ J. Jondrow, C.A.K. Lovell, I.S. Materov, and P. Schmidt in Jondrow et al. (1982).

as a single, discrete unit. With only one observation per unit, it is not possible to disentangle efficiency and time-invariant, unit-specific heterogeneity. Therefore, the presence of unobserved heterogeneity influences the estimation results of the regressors in case of correlation, or the residuals (referred to heterogeneity bias, Chamberlain (1982)). The structure of panel data offers the opportunity to apply models that account for the individual effect that should capture the unobserved heterogeneity and hence free from the heterogeneity bias. The time dimension in panel data sets allows us to observe the same unit repeatedly over a certain time span. This enables us to extract time-invariant factors such as unit-specific characteristics that do not necessarily accrue to the unit's inefficiency, but do affect the costs across different networks. Especially structural inefficiencies (inefficiency that is constant over time) and inefficiencies following a certain time path can be better identified using panel data. Most of the developments of the panel data models go back to the stochastic frontier models of Aigner et al. (1977) and Meeusen and van den Broeck (1977) expressed in Equation (3).

An early application to panel data of this stochastic frontier model was the Random Effects (RE) model by Pitt and Lee (1981) which was estimated by ML and assumed that the inefficiency u_{it} is fixed through time, but still half-normally distributed: $u_i \sim |N(0, \sigma_u^2)|$. Important variations of this model were presented by Schmidt and Sickles (1984) who relaxed the distribution assumption, and by Battese and Coelli (1988) who assumed a truncated normal distribution. Schmidt and Sickles (1984) proposed also a Fixed Effects (FE) model to avoid the possible heterogeneity bias in case of correlation of u_{it} with the explanatory variables. One of the drawbacks of models with time-invariant efficiency is that time-varying components of heterogeneity are entirely interpreted as random noise. Therefore, Cornwell et al. (1990), Kumbhakar (1990) and Battese and Coelli (1992) suggested the first stochastic models which allow the cost efficiency to vary over time. However, the first two models were vulnerable to multicollinearity and the third was characterized by a deterministic functional form of the inefficiency term over time.

The main restriction of all of the models presented above is that unobserved factors are assumed to be random over time. This implies that time-invariant factors such as physical network and environmental characteristics are not considered as heterogeneity. The family of 'true' panel data models (Kumbhakar (1991) and Polachek and Yoon (1996) as precursor models of Greene (2005) extend the original stochastic frontier model as it is formulated in Equation (3) by adding a unit-specific time-invariant factor accounting for the individual effect.¹⁶ Hence, apart from the random noise component, these models include two stochastic terms for unobserved heterogeneity, one for time-varying and one for time-invariant individual effects. This model can be written as

$$\ln C_{it} = f(\mathbf{q}_{it}; \mathbf{p}_{it}; \boldsymbol{\beta}) + \alpha_i + u_{it} + v_{it} \quad (4),$$

¹⁶ The term 'true' refers to the FE and RE models fully described in Greene (2005).

where α_i is the time-invariant unit-specific factor and the model is estimated by Maximum Simulated Likelihood (MSL). In a RE framework, α_i is an *iid* random component and must not be correlated with the observed variables. In a FE framework, α_i is a constant parameter for every unit.¹⁷ As in all ML models, the inefficiency component can be measured by the JLMS estimator of Jondrow et al. (1982). Assuming that physical network and environmental characteristics do not vary considerably over time and that the inefficiency is time-varying, these models help to separate unobserved time-invariant effects from efficiency estimates. However, if inefficiency is persistent over time, these models underestimate the inefficiency systematically, e.g. if managers take wrong decisions in every period or make the same mistakes again and again, the corresponding consequences in terms of inefficiency are detected as time-invariant unit-specific heterogeneity and not as inefficiency. As noted in Greene (2008), the ‘truth’ doubtless lies somewhere between the two strong assumptions.

The idea of observed parameter variability was early applied to a precise indication of heterogeneity of the production environment by Kalirajan and Obowona (1994) in the stochastic frontier context. A similar random parameter (RP) model was also formulated by Greene (2005), which is a generalization of the True Effects models in that not only the constant but also the parameters of the observed variables are unit-specific indicating the effect of different environments or technologies. This model is estimated by MSL. As noted by Greene (2008), the estimation of the MSL of this model can be numerically cumbersome.

Another approach to accommodate heterogeneity among units into the model is followed by latent class (LC) models. Originally introduced by Lazarsfeld and Henry (1968), LC identifies distinct class membership among subjects regarding their cost structure and estimates a separate cost function for each of these classes simultaneously.¹⁸ LC models can be regarded as the discrete counterparts of RP models. With a sufficient large number of classes, LC approximates a fully parameterized RP model. The LC model can be written as:

$$\ln C_{it} = f(\mathbf{q}_{it}, \mathbf{p}_{it}; \boldsymbol{\beta}_j) + \alpha_j + u_{it|j} + v_{it|j} \quad (5).$$

The subscript i denotes the unit, and u_{it} and v_{it} are defined as above. α_j is the constant and $\boldsymbol{\beta}_j$ is a vector of discrete random parameters identified in $j = 1, 2, \dots, J$ classes, assuming that each observation in the sample follows a specific technology. These technologies differ from each other in the values of model parameters $\{\alpha_i, \boldsymbol{\beta}_i, \sigma_i\}$. This vector includes also a set of prior probabilities that determines the fraction of each latent class in the sample. It is defined as a discrete random vector with the following distribution:

¹⁷ An alternative version of the True FE model uses dummy variables for every unit. However, this specification may be affected by the ‘incidental parameter problem’, especially in short panel data sets.

¹⁸ Latent class analysis has been applied in different fields of science and industry sectors, e.g. in the banking sector (Orea and Khumbhakar (2004)) or more recently in the electricity distribution (Cullmann (2010)).

$$\{\alpha_i, \beta_i, \sigma_i\} = \{\alpha_j, \beta_j, \sigma_j\} \text{ with probability } P_j, \text{ where: } j = 1, 2, \dots, J, \text{ and } \sum_{j=1}^J P_j = 1 \quad (6).$$

The subscript j denotes the latent class with J being the number of classes. The choice of J is usually based on diagnostic criteria such as the Akaike Information Criterion (AIC) or the Bayesian Information Criterion (BIC).¹⁹ These criteria indicate the optimal number of classes from an informational perspective, but cannot be used for statistical inference. After the estimation of the LC model, posterior probabilities P_j can be calculated for each observation from Bayes rule.

The choice of the econometric models presented so far is usually not straightforward. For instance, Farsi and Filippini (2009) have found several studies that report discrepancies in efficiency estimates between different models and approaches.²⁰ Such discrepancies are partly due to methodological sensitivity in the estimation of individual efficiency scores and partly due to different consideration of unobserved heterogeneity factors, which is particularly relevant in network industries such as electricity distribution. Panel data models can be used to control for the firm- or network specific unobserved heterogeneity. The use of panel data models is especially interesting as data for several years have become available to an increasing number of regulators in many countries. The complexity of such models remains however as an important obstacle in applying panel data models in regulation. The effort in disentangling inefficiency variations from unobserved factors such as statistical noise due to error and omitted variables is a crucial element of all frontier models, in both cross sectional and panel data. The statistical modeling challenge has a parallel in practice: Benchmarking can only be effective to the extent that for any specific company with given characteristics, there exists a set of comparable companies upon which a ‘best practice’ can be constructed.

Therefore, as discussed previously, we propose in this paper an alternative strategy to consider unobserved heterogeneity factors in that we decompose the benchmarking analysis into two steps: In the first step, we attempt to identify classes of companies that operate in similar environments and with comparable network and structural characteristics. For that step, we use a latent class model. In the second step, best practice is obtained within each class applying different benchmarking methods. Provided that the identified classes include reasonably comparable cases and assuming a reasonable explanatory power for the variables included in the model specification, any deterministic or stochastic approach can provide accurate values of efficiency. Therefore, we use the DEA, MOLS and SFA

¹⁹ However, compared to the BIC, the AIC corrects the likelihood function only by the sample size and not by the number of parameters to estimate. This is a clear disadvantage with increasing number of classes.

²⁰ See e.g. Jensen (2000), Jamasb and Pollitt (2003), Street (2003), Estache et al. (2004), Farsi and Filippini (2004). The results show substantial variations in estimated efficiency scores and, for some of them, in efficiency rankings across different approaches (econometric and non-parametric) and among model specifications.

methods for the second step. In the next section, we will apply this approach using a sample of Norwegian electricity distribution companies.

3 COST MODEL SPECIFICATION AND ESTIMATION METHODS

We specify a cost model that explains total costs of the Norwegian electricity distribution system operators (DSO) with two input and one output variable, one environmental and one network characteristics. We write this model as follows:

$$TC = f(P_L, P_C, Q, D, LS) \quad (7),$$

where the dependent variable TC represents the total costs of the DSO. P_L and P_C are the input prices of labor and capital, respectively. Q is the delivered electricity, D the network density and LS , finally, the share of high voltage network. For a complete description of the data and variables, see Section 4.

For the identification of the comparable technology classes in the first step, we apply a Latent Class (LC) approach (cf. Lazarsfeld and Henry (1968), see Section 2)²¹ to estimate cost model in Equation (7).²² Using a Cobb-Douglas functional form and imposing the linear homogeneity restriction, the LC model in Equation (5) can be adapted to:

$$\ln \frac{TC_{it}}{P_{Cit}} = \alpha_{0j} + \beta_{Pj} \ln \frac{P_{Lit}}{P_{Cit}} + \beta_{Qj} \ln Q_{it} + \beta_{Dj} \ln D_{it} + \beta_{LSj} LS_{it} + \varepsilon_{it|j} \quad (8),$$

where subscript i denotes the electricity distribution company $i = 1, 2, \dots, I$, subscript t the years 1998 – 2002, and $\varepsilon_{it} \sim N(0, \sigma_i)$ the error term. The subscript j denotes the latent class with J being the number of classes.

After the identification of comparable technology classes, we estimate the cost efficiency in the second step separately for each class. As the heterogeneity within classes is expected to be low due to comparable technologies, any deterministic or stochastic approach can be considered. For general overviews on approaches to efficiency measurement, see e.g. Murillo-Zamorano (2004) or Greene (2008), or, for an empirical application, Farsi and Filippini (2009). With respect to current regulatory practice (see Haney and Pollitt (2009) for an overview over 40 countries), we apply the three following, most prevalent methods: The Data Envelopment Analysis (DEA, proposed by Farrell (1957) and Charnes et al. (1978)), the Modified OLS (MOLS, proposed by Afriat (1972)) and the Stochastic Frontier Analysis (SFA, proposed by Aigner et al. (1977)).

²¹ Different models could be considered to identify technology classes. LC is a statistical method that has been used in literature to identify classes (see Orea and Khumbhakar (2004) or Greene (2005)).

²² All estimations have been conducted by Nlogit software version 4.0.

The DEA is a non-parametric method to calculate cost efficiency as a deterministic function of the observed variables, i.e. it is assumed that the data are free of stochastic variation due to measurement errors or noise. The cost model given in Equation (7) can be readily used for the efficiency measurement with the DEA method. Assuming variable returns to scale (VRS), the Equation (1) reduces to the following minimization problem:

$$\begin{aligned} & \min_{\lambda} TC_{it} \\ s.t.: & \quad -Y_{it} + Y\lambda \geq 0; \quad TC_{it} - TC\lambda \geq 0; \quad N'\lambda = 1; \quad \lambda \geq 0 \end{aligned} \quad (10),$$

where Y_{it} represents the vector of the output bundle including output Q_{it} and output characteristics D_{it} and LS_{it} , as both characteristics take resources. However, in the DEA model, D is defined as the inverse of the network density, since a higher network density implies lower costs. N and λ are vectors of ones and non-negative constants, respectively. Cost efficiency (CE) is measured as the minimum feasible costs for each company relative to its actual costs, i.e. $CE_{it} = TC^*/TC_{it}$.

The MOLS and the SFA are parametric methods that use regression techniques to construct the efficiency frontier. Both require the specification of a functional form of the cost function as well as assumptions about the error term(s). Similar to Equation (8) in the first step, we estimate cost model in Equation (7) using a Cobb-Douglas functional form and impose the linear homogeneity restriction. The MOLS and SFA models in Equations (2) and (3) can be adapted to:

$$\ln \frac{TC_{it}}{P_{Cit}} = \alpha_0 + \beta_p \ln \frac{P_{Lit}}{P_{Cit}} + \beta_Q \ln Q_{it} + \beta_D \ln D_{it} + \beta_{LS} LS_{it} + \varepsilon_{it} \quad (11).$$

The MOLS approach is based on the OLS estimation. The residuals ε_{it} are corrected using a constant shift, which is the expected value of the inefficiency term, $E(u_{it})$. The cost efficiency in the MOLS is thus deterministic and given by $CE_{it} = \exp(-u_{it})$ with $u_{it} = \varepsilon_{it} + E(u_{it})$. u_{it} is not necessarily positive, as some units may lie below the cost frontier. Truncation at zero assigns the respective units with full efficiency.

The SFA approach is based on the Maximum Likelihood estimation. The residuals ε_{it} are composed of the inefficiency term u_{it} and the random noise term v_{it} . In this study, it is assumed that u_{it} follows one-sided non-negative distribution, i.e. a normal distribution truncated at zero: $u_{it} \sim |N(0, \sigma_u^2)|$, and that v_{it} is normally distributed: $v_{it} \sim N(0, \sigma_v^2)$. Additionally, u_{it} and v_{it} are considered as being independently distributed from each other. The cost efficiency in the SFA is thus stochastic and given by $CE_{it} = \exp(-u_{it})$.

In order to compare the results from this two step approach with that of a conventional analysis, we estimate the three models (DEA, MOLS, SFA) also in one step, i.e. without consideration of classes, but for the whole sample. The according tables are given in the Appendix.

4 DATA

The data we use for this study consists of a balanced panel of 555 observations from 111 companies that have operated in the Norwegian power distribution sector from 1998 to 2002.²³ The available information includes total costs, labor costs, full time equivalents, total transformer capacity, distributed electricity, number of customers, line length for each low and high voltage, and year dummies. Table 1 provides a descriptive summary of the balanced panel data set for the variables included in the models.

Table 1: Descriptive summary, 1998-2002

Variable description	Variable	Mean	Std.dev.	Min	p25	Median	p75	Max
Total cost (10^6 NOK)	TC	36.5	73.4	1.28	11.7	18.1	35.8	862
Labor cost (10^6 NOK)		10.2	16.8	0.47	3.70	5.58	10.2	161
Fulltime equivalents (FTE)		30.0	48.9	2.00	10.0	16.0	31.0	419
Price labor (10^3 NOK/ FTE)	P_L	349	52.9	120	312	344	383	586
Transformer capacity (MVA)		243	698	4.08	38.8	75.7	201	7'944
Price capital (10^3 NOK/ MVA)	P_C	176	83.6	31.6	112	160	220	528
Distributed electricity (GWh)	Q	316	942	6.86	66.4	127	267	11'200
Number of customers		11'445	32'622	288	2'812	5'002	10'176	373'290
Line length (km)		1'351	1'871	56.5	467	762	1'609	13'583
Density ($customers/km$)	D	7.00	3.25	1.32	5.16	6.23	7.66	29.0
Line length, high voltage (km)		492	703	10.0	159	267	557	4'995
Line length, low voltage (km)		859	1'209	0.00	292	493	930	10'090
Line length, high voltage share	LS	0.37	0.11	0.09	0.30	0.36	0.43	1.00
Year dummies	$dyear$	0.20	0.40	0.00	0.00	0.00	0.00	1.00

T = 5 (panel of years 1998-2002), i = 111, N = 555

From these variables, we calculated the variables included in the models as follows: The dependent variable (TC) is the total network costs excluding the cost of purchased electricity. It is measured in millions Norway Kroner (NOK) and is in real terms; hence it is adjusted for inflation. TC includes all DSO's network costs consisting of both operating and capital expenditures. The explanatory variables involve two input price variables, one output variable and one environmental and one network characteristic, hence the DSO's here are considered to be single-product firms. The input price variables include a price for labor (P_L) and a price for capital (P_C). We derived P_L by

²³ In order to get a balanced panel data set, we extracted this data from the data that has been used in several scientific studies (Agrell et al. (2005a) and (2005b)) as well as in a research project financed by the Norwegian Water Resources and Energy Directorate partly reported in Agrell and Bogetoft (2009) and a research project financed by Swiss Federal Institute of Energy reported in Filippini et al. (2012).

dividing labor costs by the number of full-time equivalents. P_C is an approximation to the real capital price, calculated as a residual price by dividing non-labor costs by the installed transformer capacity. The output is given by the delivered electricity (Q), measured in Giga Watt-hours (GWh). The environmental variable is the network density (D), represented by total number of customers divided by total network length in kilometers. The network characteristic (S) is modeled by the share of high voltage network length and total network length.

5 RESULTS

In the first step, we first determine the optimal number of classes J of the LC model. Using model specification in Equation (8), we applied LC models to the data in Table 1 with two to six classes.²⁴ The specification diagnostics obtained by this analysis show that $J=4$ is the optimal number of classes for the BIC and $J=6$ for the AIC. In cases with $J>4$, we observed some implausible values for regression coefficients, e.g. statistically insignificant values for the output. Considering the interesting statistical features of the BIC, we adopted this criterion and selected four classes.

The estimation results of this LC model estimated in the first step are summarized in Table 2. These results show four distinctive technology classes with significant coefficients in most of the cases. Differences in the coefficients indicate that there are variations in marginal costs and technological characteristics across these classes. We see throughout all classes that total cost increase with higher input prices and higher outputs and in three classes with an increasing share of high voltage networks. As expected, operation with density reduces costs. Differences in coefficients indicate that there are variations in marginal costs and technical characteristics across classes. Prior class probabilities indicate also different class sizes.

Table 2: Estimation results latent class model with four classes, first step

First step Variable	Class 1 Coefficient (SE)	Class 2 Coefficient (SE)	Class 3 Coefficient (SE)	Class 4 Coefficient (SE)
Input price ratio (P)	0.8581 *** (0.034)	0.4591 *** (0.020)	0.8675 *** (0.028)	0.6869 *** (0.014)
Distributed electricity (Q)	0.9083 *** (0.016)	0.7752 *** (0.008)	1.0600 *** (0.016)	0.9871 *** (0.008)
Density (D)	-0.4228 *** (0.052)	-0.3301 *** (0.026)	-0.9295 *** (0.067)	-0.0537 *** (0.020)
Share HV network (S)	0.5928 *** (0.153)	0.0875 (0.107)	2.7845 *** (0.197)	0.7600 *** (0.056)
Constant	5.0126 *** (0.016)	4.6728 *** (0.007)	4.6591 *** (0.012)	4.7313 *** (0.006)
Sigma (σ^2)	0.1939 *** (0.009)	0.0739 *** (0.005)	0.0939 *** (0.009)	0.0804 *** (0.004)
Prior class probability	0.2157 *** (0.040)	0.2833 *** (0.046)	0.1752 *** (0.039)	0.3258 *** (0.048)

***, **, *: significant at 1%, 5% and 10%, respectively; standard errors given in brackets. T = 5 (panel of years 1998-2002), i = 111, n = 555

²⁴ Using several specifications, we also tried models with seven or more classes. Due to non-convergence we could not estimate any models with more than six classes.

Table 3 provides a descriptive summary of the observed variables for each class as identified by the estimated posterior class probabilities. These probabilities show that the companies can be distinguished with high probabilities. The fact that even in the worst cases, minimum probabilities are greater than 0.5, suggest that companies can be classified without much suspicion. The resulting classes have at least 100 observations, which is large enough for reasonable degrees of freedom for the second step estimations. The values of the observed variables in each class indicate that we can distinguish in an approximate manner certain features that characterize each class. Class 1 faces low input prices and a high customer density, whereas class 2 has high input prices and medium customer density. Classes 3 and 4 face medium values for most of the variables except for a relatively low customer density in class 3.

Table 3: Identifying the classes

Variable description	Variable	Sample	Class 1	Class 2	Class 3	Class 4
Posterior class probability			0.99 (0.01)	0.91 (0.12)	0.91 (0.16)	0.98 (0.04)
Total cost (10^6 NOK)	TC	36.5 (73.4)	65.2 (136)	14.5 (7.09)	45.9 (67.0)	33.5 (36.7)
Price labor (10^3 NOK/FTE)	P_L	349 (52.9)	338 (53.5)	355 (53.9)	352 (55.5)	348 (49.2)
Price capital (10^3 NOK/MVA)	P_C	176 (83.6)	155 (81.0)	213 (92.4)	166 (76.2)	161 (67.3)
Distributed electricity (GWh)	Q	316 (942)	675 (1936)	109 (90.6)	332 (454)	272 (345)
Density (customers/km)	D	7.00 (3.25)	7.84 (5.15)	6.92 (2.91)	6.28 (1.49)	6.92 (2.49)
Line length, high voltage share	LS	0.37 (0.11)	0.36 (0.10)	0.37 (0.13)	0.38 (0.07)	0.38 (0.09)
Standard errors given in brackets.	N	555	115	170	100	170

The estimation results for the MOLS and the SFA estimated in the second step for each class separately are summarized in Table 4. Other than the first step, the estimations are based on cost model specification in Equation (11) and on subsamples of the data in Table 1, given by the four classes of the first step. In general, the coefficients are of the same magnitude as in the LC model in the first step. The coefficients of the MOLS and the SFA differ slightly because of different assumptions on the error term. The signal-to-noise ratio λ is significant for three classes indicating skewness and existence of inefficiency. The insignificant value of λ in class two means that standard errors of the inefficiency terms are low compared to that of the noise terms, which will result in low inefficiency values for this class.

Table 4: Estimation results MOLS and SFA for each class, second step

Second step		Class 1		Class 2		Class 3		Class 4	
Variable		Coefficient (SE)		Coefficient (SE)		Coefficient (SE)		Coefficient (SE)	
MOLS	Input price ratio (P)	0.8588 *** (0.048)	0.4623 *** (0.018)	0.8644 *** (0.023)	0.6891 *** (0.018)				
	Distributed electricity (Q)	0.9080 *** (0.020)	0.7719 *** (0.010)	1.0581 *** (0.010)	0.9856 *** (0.008)				
	Density (D)	-0.4236 *** (0.056)	-0.3252 *** (0.017)	-0.9255 *** (0.055)	-0.0464 ** (0.019)				
	Share HV network (S)	0.6076 *** (0.202)	0.0802 (0.050)	2.7761 *** (0.164)	0.7582 *** (0.072)				
	Constant	5.0162 *** (0.019)	4.6692 *** (0.007)	4.6642 *** (0.010)	4.7317 *** (0.007)				
SFA	Input price ratio (P)	0.8961 *** (0.050)	0.4624 *** (0.017)	0.8669 *** (0.022)	0.6880 *** (0.018)				
	Distributed electricity (Q)	0.9027 *** (0.020)	0.7719 *** (0.010)	1.0587 *** (0.010)	0.9867 *** (0.008)				
	Density (D)	-0.4140 *** (0.055)	-0.3253 *** (0.017)	-0.9329 *** (0.053)	-0.0469 ** (0.019)				
	Share HV network (S)	0.8017 *** (0.188)	0.0802 (0.049)	2.7953 *** (0.161)	0.7538 *** (0.071)				
	Constant	4.8158 *** (0.020)	4.6472 *** (0.015)	4.6079 *** (0.016)	4.6947 *** (0.011)				
	Sigma: $\sigma^2 = \sigma_u^2 + \sigma_v^2$	0.2786 *** (0.002)	0.0764 *** (0.000)	0.1082 *** (0.001)	0.0870 *** (0.000)				
	Lambda: $\lambda = \sigma_u / \sigma_v$	2.1775 *** (0.395)	0.3866 (0.265)	0.8413 *** (0.275)	0.6256 *** (0.214)				

***, **, *: significant at 1%, 5% and 10%, respectively; standard errors given in brackets. T = 5 (panel of years 1998-2002), i = 111, N = 555

The results of the efficiency analysis for the four classes and three models each are summarized in Table 5. The average efficiency value ranges from 0.56 for DEA in Class 1 to 0.98 for SFA in Class 2. In general, the average efficiency values are lowest in Class 1 for all three models and highest in Class 2 for MOLS and SFA. The highest average efficiency value for DEA is in Class 3 with 0.81. The standard deviations are highest in Class 1 for all three models and lowest in Class 2 for SFA, indicated already by the insignificant lambda in Table 4. Throughout all three models, SFA produces higher efficiency values than DEA and MOLS. This is expected since the model considers statistical noise. Another typical feature is that whereas DEA and MOLS assign full efficiency to several observations, SFA does not classify any operator as fully efficient. The minimum values are low in Class 1 for all three models. In particular, DEA attributes considerable lower minimum values for all classes than the other models.

Table 5: Efficiency scores, second step

	Class 1			Class 2			Class 3			Class 4		
	DEA	MOLS	SFA									
Mean	0.568	0.776	0.829	0.695	0.906	0.978	0.807	0.882	0.946	0.771	0.899	0.964
SDev	0.207	0.131	0.093	0.168	0.062	0.006	0.149	0.076	0.018	0.125	0.065	0.010
Min	0.267	0.362	0.531	0.374	0.732	0.916	0.481	0.695	0.883	0.559	0.740	0.933
p25	0.429	0.702	0.793	0.559	0.860	0.976	0.680	0.836	0.939	0.682	0.861	0.960
Median	0.496	0.773	0.843	0.652	0.902	0.978	0.799	0.881	0.950	0.743	0.895	0.965
p75	0.688	0.854	0.890	0.832	0.954	0.981	0.958	0.938	0.959	0.860	0.947	0.971
Max	1	1	0.962	1	1	0.986	1	1	0.976	1	1	0.983

T = 5 (1998-2002), i = 111, N = 555

In general, the efficiency values are higher and more realistic than the corresponding scores of a conventional analysis performed in one step (given in Table 7 in the appendix). The decomposition of the benchmarking process into two steps and the consideration of technology classes has reduced unobserved heterogeneity within classes and, hence, reduced the unexplained variance previously claimed as inefficiency. Therefore, conventional cross-sectional or pooled models might underestimate cost efficiency.

6 SUMMARY AND CONCLUSIONS

Regulatory authorities increasingly use benchmarking practices to identify a company's individual efficiency in various incentive regulation schemes such as price- or revenue cap. The identification of cost efficiency in electricity distribution is a challenging task, as the companies operate in different regions with various environmental and network characteristics that are only partially observed. Therefore, the purpose of this study was to analyze cost efficiency in electricity distribution under consideration of these unobserved heterogeneity factors.

In order to disentangle cost efficiency variations from unobserved factors, we proposed an alternative strategy that decomposes the benchmarking process into two steps: The first step is to identify classes of comparable companies in order to reduce unobserved heterogeneity within classes and the second to obtain the best practice for each class.

The analysis in the first step has revealed four distinct latent classes. These classes can be characterized in an approximate manner by different observed variables, mainly by input prices and customer density. The analysis in the second step applying DEA, MOLS and SFA frontier methods has shown that average efficiency values vary considerably among methods and classes. In general, DEA has produced lowest and SFA highest values. Companies in class 1 are on average considerably less efficient than companies in the other classes, and the variation in efficiency scores in class 1 is highest. This class involves clearly the largest and most heterogeneous companies concerning output.

Most importantly, the efficiency values are generally higher and more realistic than the corresponding scores of a conventional analysis performed in one step. The decomposition of the benchmarking process into two steps and the consideration of technology classes has reduced unobserved heterogeneity within classes and, hence, reduced the unexplained variance previously claimed as inefficiency. Therefore, conventional cross-sectional or pooled models might underestimate the real cost efficiency values. This in turn could lead to too incommensurate regulatory measures in account of the affected companies, especially if price or revenue cap regulation as incentive regulation scheme is in force.

APPENDIX

Table 6: Estimation results for MOLS and COLS, conventional analysis

Variable	MOLS		SFA	
	Coefficient	(SE)	Coefficient	(SE)
Input price ratio (P)	0.6827 ***	(0.024)	0.6637 ***	(0.024)
Distributed electricity (Q)	0.9328 ***	(0.011)	0.9327 ***	(0.011)
Density (D)	-0.3423 ***	(0.028)	-0.3226 ***	(0.024)
Share HV network (S)	0.7258 ***	(0.091)	0.7679 ***	(0.080)
Constant	4.8223 ***	(0.009)	4.5888 ***	(0.011)
Sigma: $\sigma^2 = \sigma_n^2 + \sigma_v^2$			0.3175 ***	(0.001)
Lambda: $\lambda = \sigma_u / \sigma_v$			2.2973 ***	(0.229)
***, **, *: significant at 1%, 5% and 10%, respectively.				N = 555

Table 7: Efficiency scores, conventional analysis

	DEA	MOLS	SFA
Mean	0.554	0.762	0.802
SDev	0.151	0.148	0.104
Min	0.246	0.319	0.498
p25	0.453	0.645	0.727
Median	0.527	0.769	0.827
p75	0.625	0.871	0.887
Max	1	1	0.960
T = 5 (1998-2002), i = 111, N = 555			

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